

How We Know What We Know

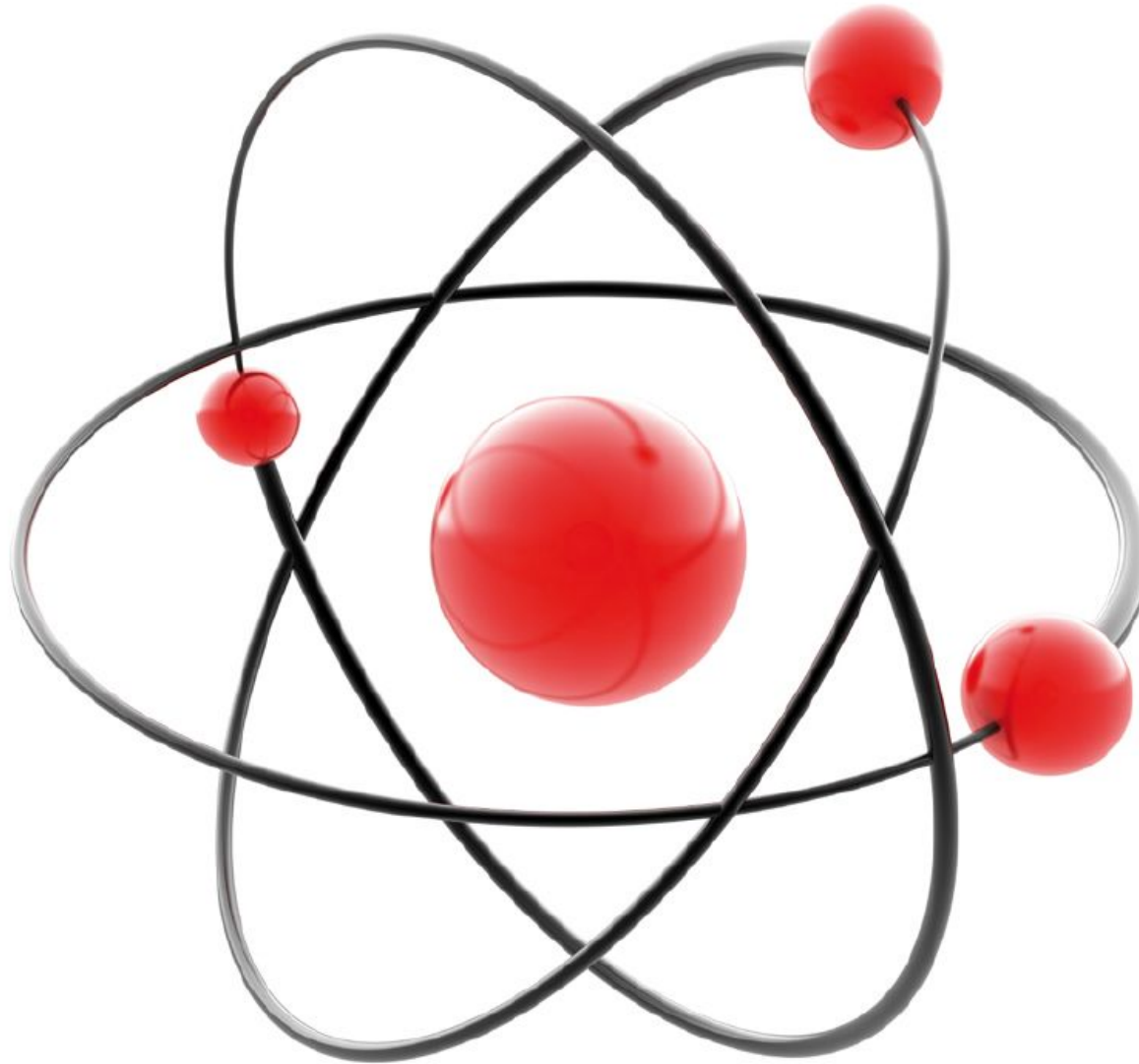
Chris Sorensen

Physics

Kansas State University

Callanish Standing Stones, Lewis, Scotland
Earliest construction at this site dates to 3000 BC
Photo by Dave Rintoul, Kansas State University

How do we know atoms exist?



Ancient Speculations

The Atomic Hypothesis

Leucippus and Democritus, ca. 400 BC

What if...

You cut a piece of iron in half?

“a-tomic” Greek for “non-divisible”



Democritus

wikipedia

Let's go dancing!

Dance 1. A ton of girls and a ton of boys.

After the dance, we find some changes.

There is now a new compound called “couples”
and there is 1.5 ton of couples.

We also find 0.5 ton of girls left over.

Dance 2. 1 ton of girls and 3 tons of boys.

After the dance, there is 3 tons of couples.

We also find 1 ton of boys left over.

Dance 3. 1 ton of girls and 2 tons of boys.

After the dance, there is 3 tons of couples,
and no one is left over.

Conclusion (not unique): Boys and girls combine in a
2:1 mass ratio to make couples. Why? Maybe girls and boys
come in indivisible pieces of fixed mass with that ratio.

Let do some chemistry!! (and solve some puzzles)

React 1 gram of hydrogen (H) with lots of oxygen (O)
you get 9 grams of water and lose 8 grams of O.
i.e. 1 gram of H combines with 8 grams of O

Implies the “pieces” of O are 8 times as massive as
the “pieces” of H

React 1 gram H with lots of O and lots of sodium (Na).
You get 40 grams of lye and lose 16 grams of O
and 23 grams of Na.

This time 1 gram of H combines with 16 grams of O

Maybe the “pieces” of O are 16 times more massive than H,
and water had 2 H “pieces” for every O “piece”.

John Dalton ca. 1800

The Laws of Definite and Multiple Proportions

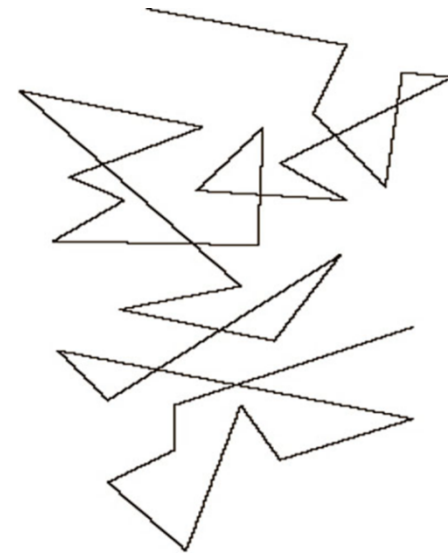
These laws imply that
matter comes in “pieces”
called atoms



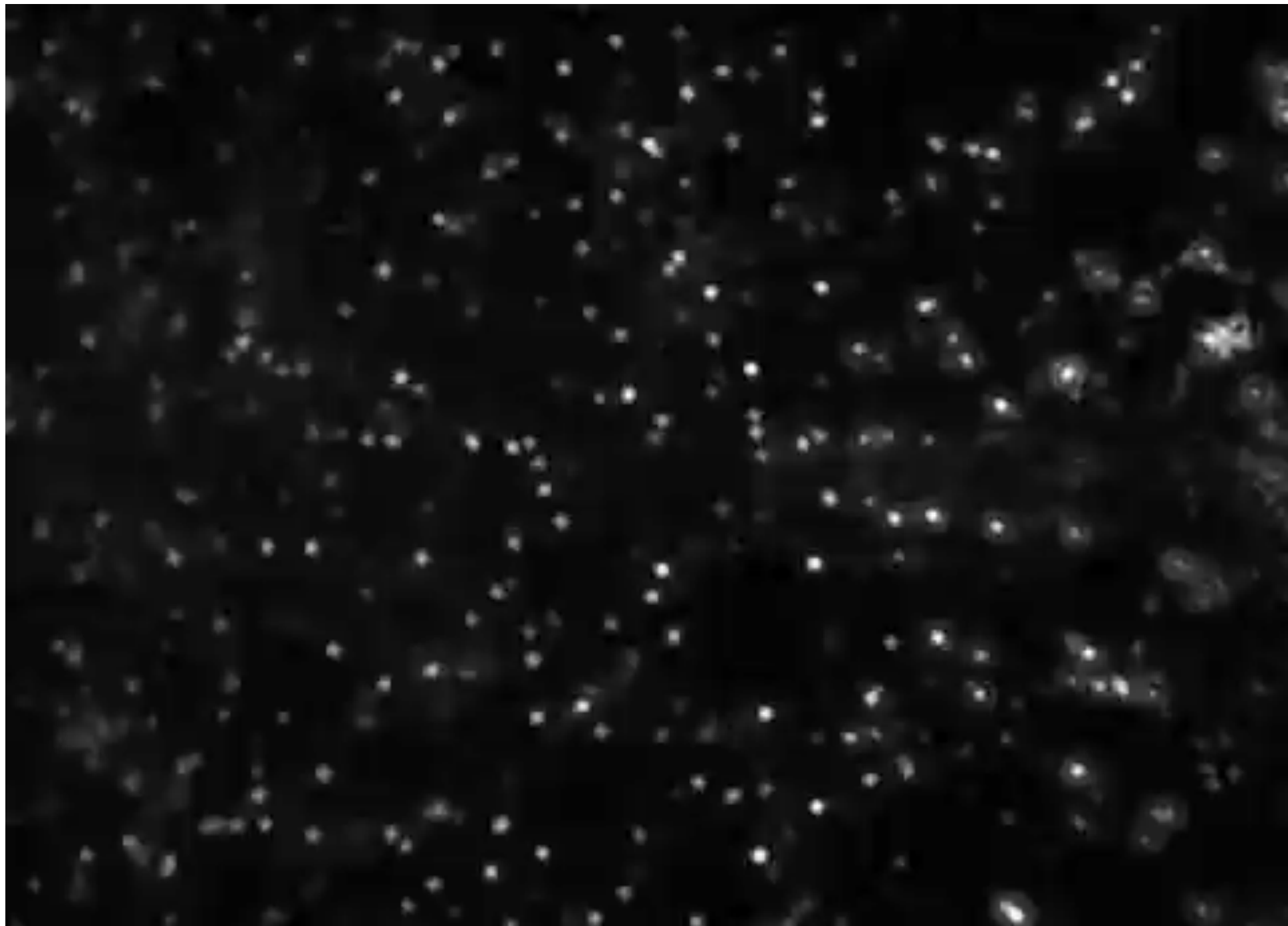
Brownian Motion

In 1827 Robert Brown, looking through a microscope at pollen grains in water, noted that the grains moved randomly through the still water.

Why?



Random Path



Einstein (1905): the thermal motion of atoms!

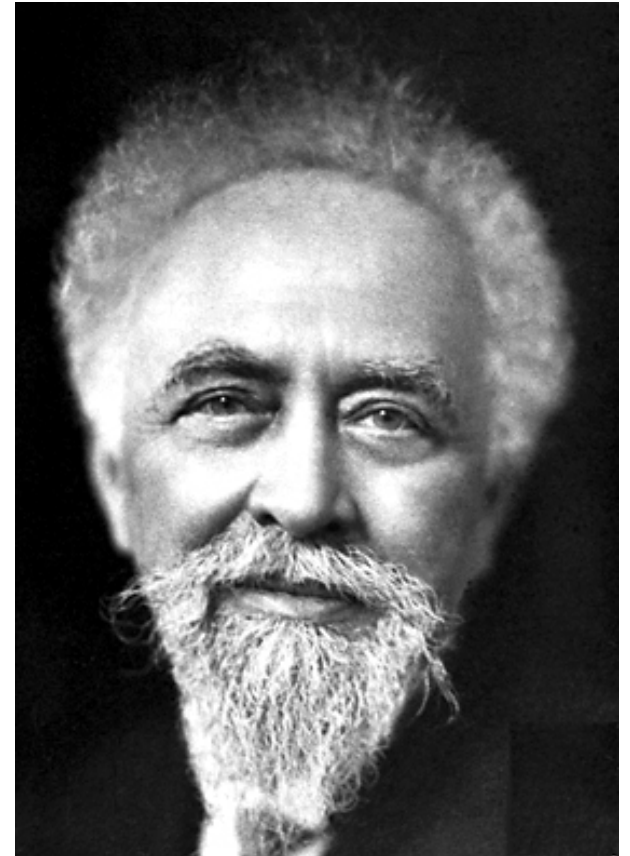
Physical scientists of this pivotal period [early 20th century] did not for one minute assume ... the discontinuity of the matter which underlies visible reality. In looking back upon the discoveries and theories of particles, one perhaps fails to realize that the focus was not simply upon the nature of the molecules, ions and atoms, but upon the very fact of their existence...

Mary Jo Nye

Einstein 1905

Perrin 1909

Bohr 1913



The Nobel Prize in Physics 1926

Jean Baptiste Perrin for his work on *the discontinuous structure of matter, and especially for his discovery of sedimentation equilibrium*".

The Kinetic Theory of Heat

Boltzmann, ca. 1900

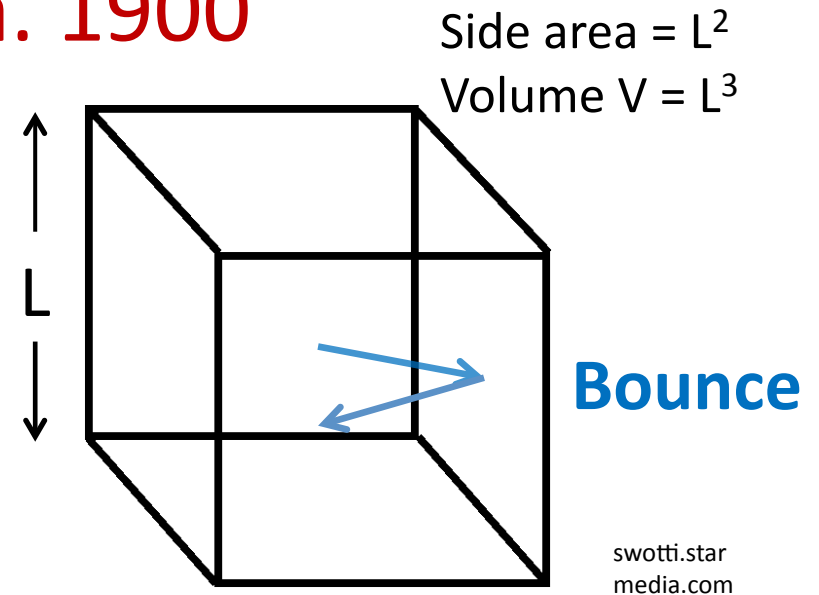
Heat is atomic motion

An atom of mass m
has a kinetic energy given by

$$E = mv^2/2 = 3kT/2$$

k is Boltzmann's constant

T is the temperature (absolute).



Pressure P due to bounce

Bounces increase with number of atoms, $P \sim N$

decrease with time between bounces, $P \sim 1/V$

become stronger with atom energy, $P \sim kT$

Thus $P \sim NkT/V$, The Ideal Gas Law!

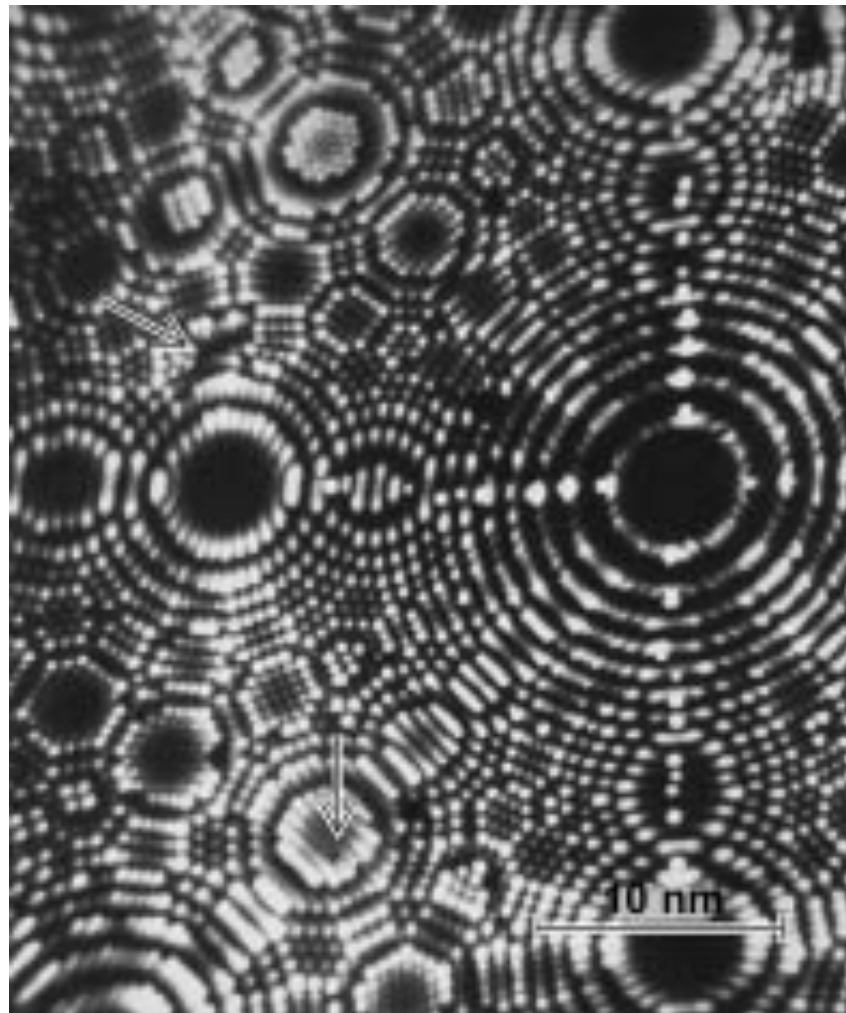
Boltzmann



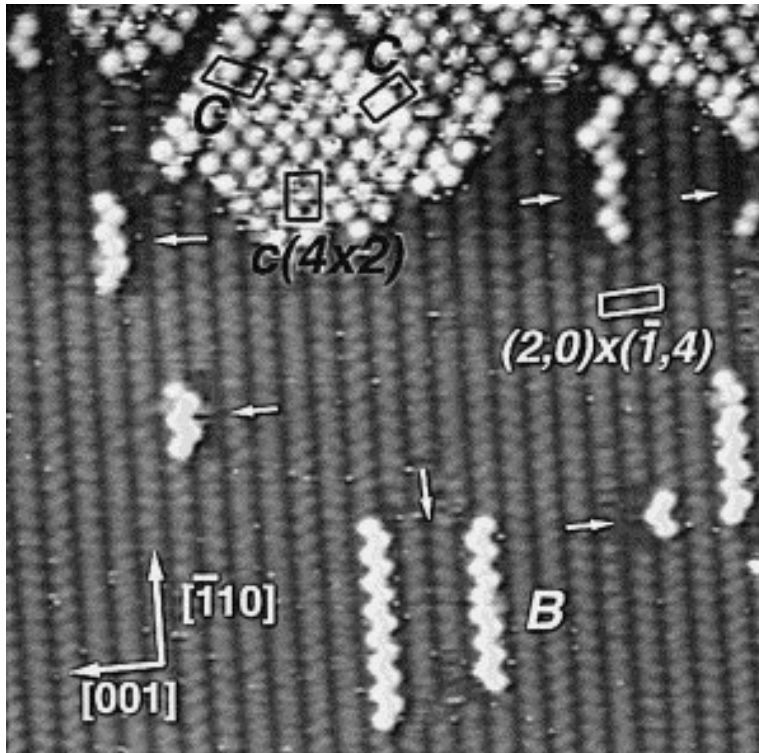
[wikipedia.org/wiki/
File:Zentralfriedhof_Vienna_-
_Boltzmann.JPG](https://wikipedia.org/wiki/File:Zentralfriedhof_Vienna_-_Boltzmann.JPG)

Fielded-Emission Microscope

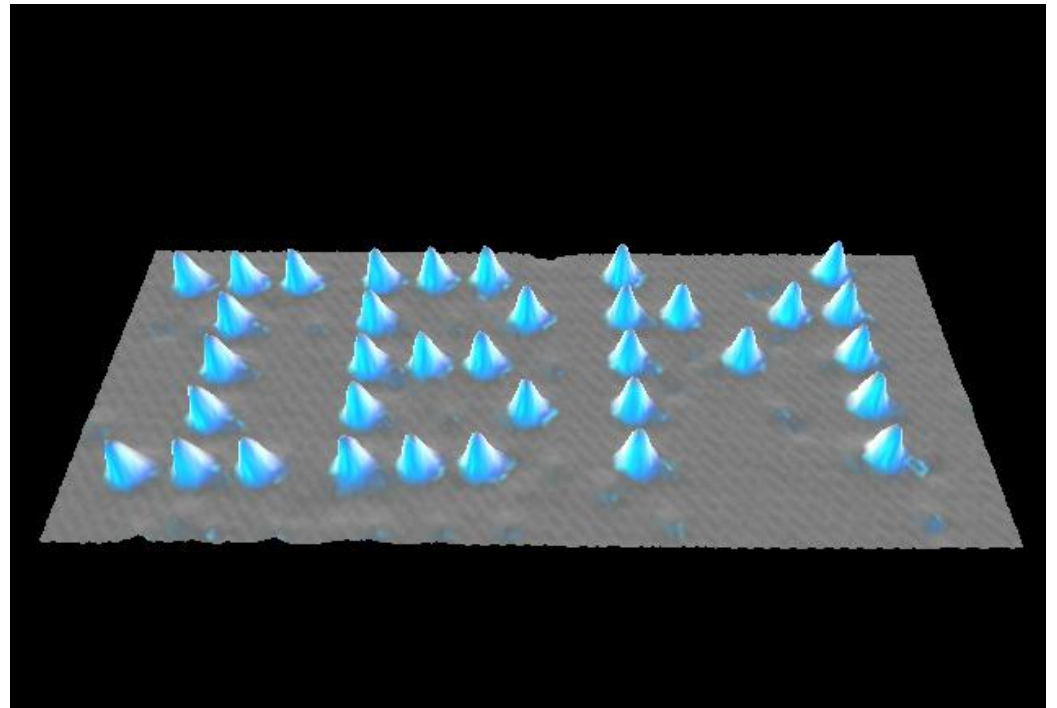
Ca. mid 20th Century



Scanning Tunneling Microscope

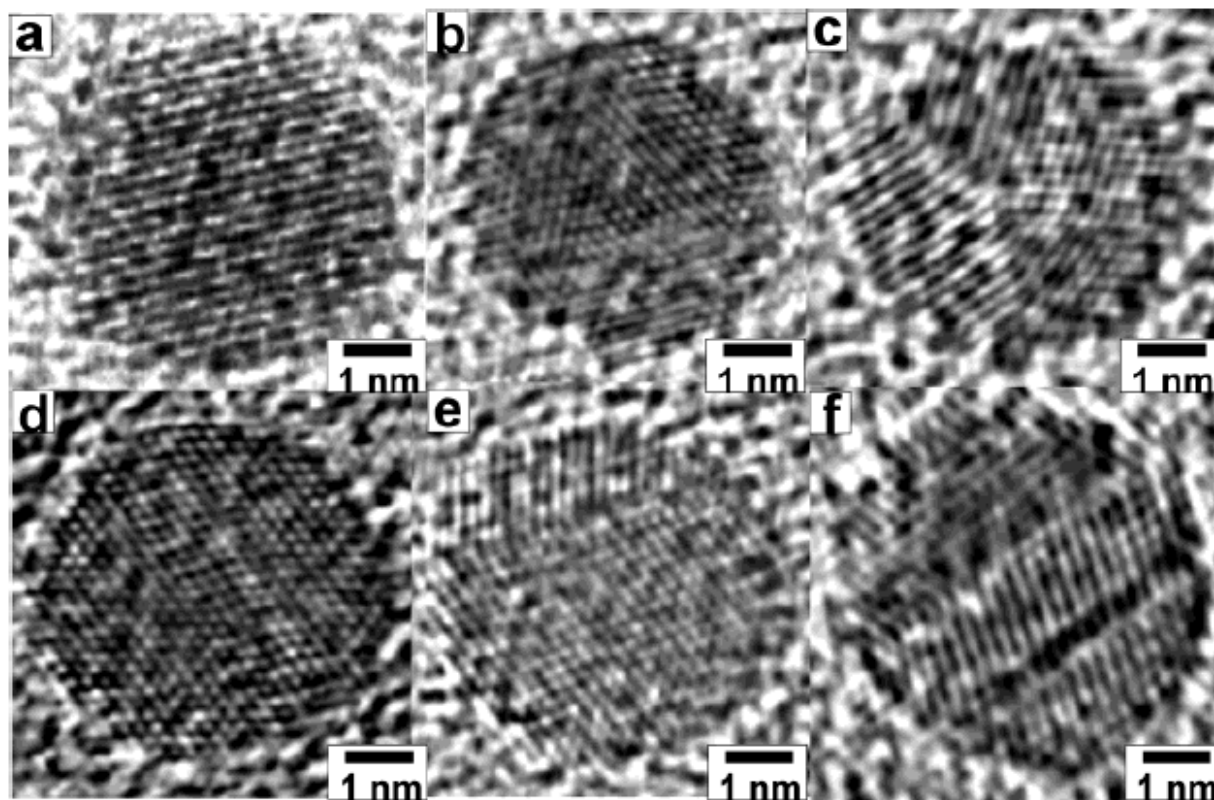


Tin atoms (white) on
Silicon surface (grey)



Xenon atoms manipulated to
Spell IBM on silicon (unresolved).

High Resolution Transmission Electron Microscopy HRTEM



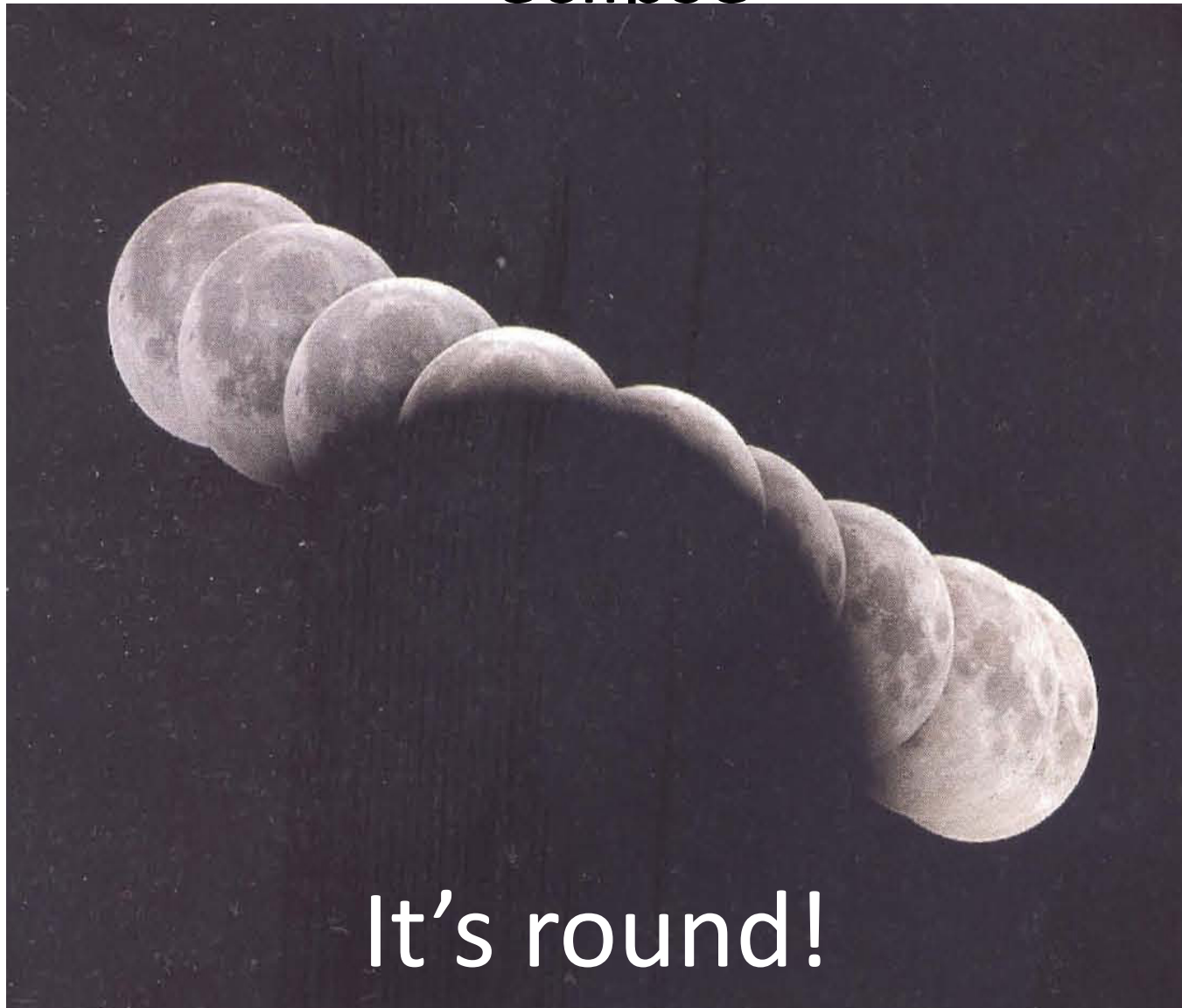
Gold nanoparticles. Individual dots are gold atoms

Seeing is believing ... I guess

How big is the Earth?



The Earth's shadow during a lunar eclipse

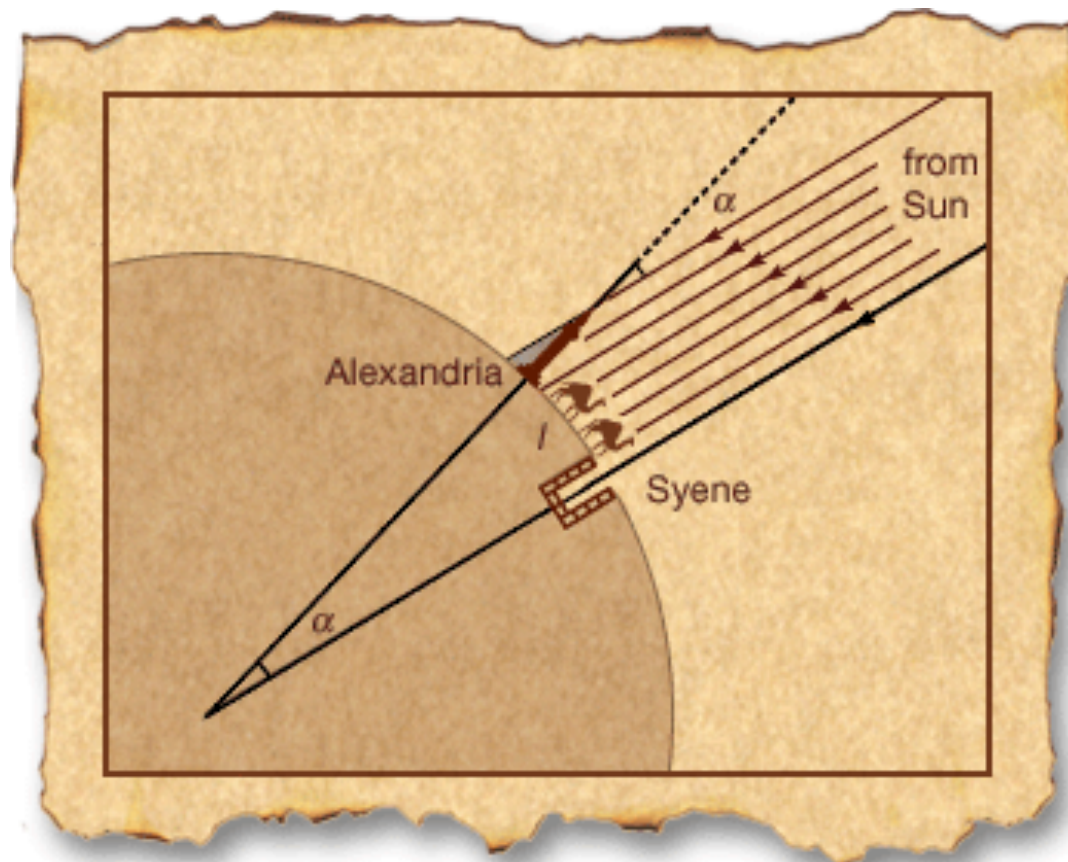


It's round!

Eratosthenes

Measuring the Earth

Ca. 250 BC



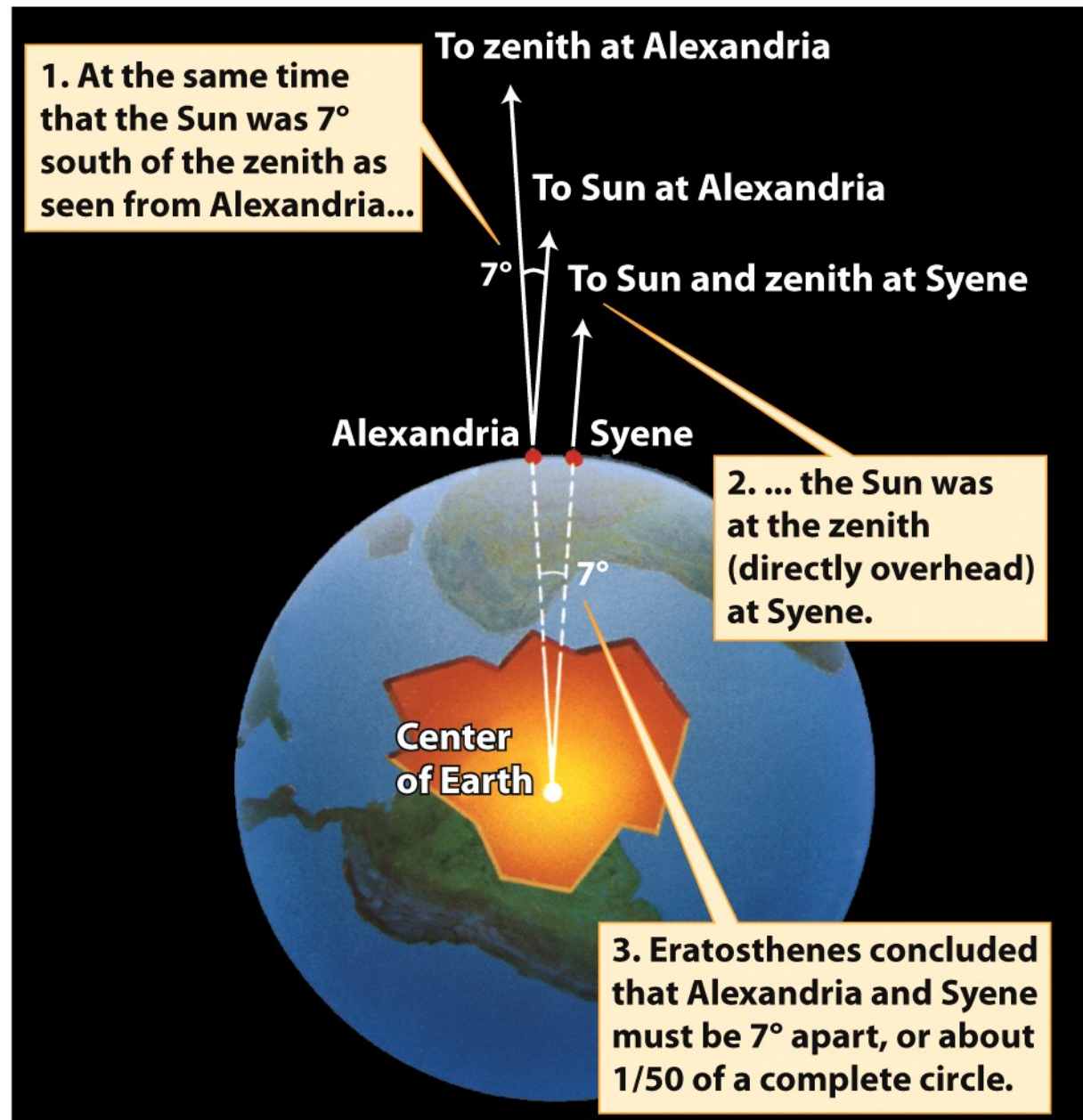


Figure 3-1
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Weighing the Earth

Know the size, i.e. radius R (Eratosthenes ...)

Guess the density, e.g. water at $\rho = 1.0 \text{ g/cc}$.

Calculate the mass:

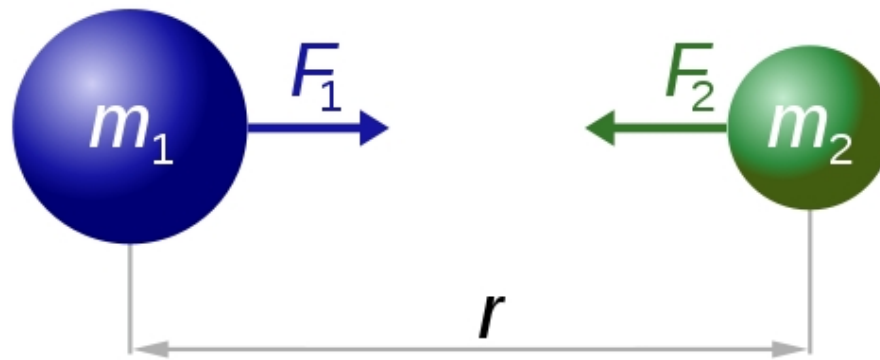
$$M = \rho \frac{4\pi R^3}{3}$$

$$M = 10^3 (12.56) (6.38 \times 10^6)^3 / 3 \quad (\text{SI units})$$

$$M = 1.1 \times 10^{24} \text{ kg}$$

Weighing the Earth (2)

Newton's Law of Universal Gravitation



$$F_1 = F_2 = G \frac{m_1 \times m_2}{r^2}$$

What is Big G?

The Physics of Falling

Ball



$$F = Gm_b M_E / r^2$$

Earth/ball distance is
Center-to-center distance

$$r = R_E$$

Newton's 2nd Law

$$F = ma$$

Combine

$$m_b a = Gm_b M_E / R_E^2$$

$$a = GM_E / R_E^2$$

And what is the acceleration a ?

It's the acceleration of gravity $g = 9.8\text{m/s}^2$!

$$\text{Thus, } M_E = gR_E^2 / G$$

*Leaning Tower
of Kansas*



The Cavendish Experiment

1797-98

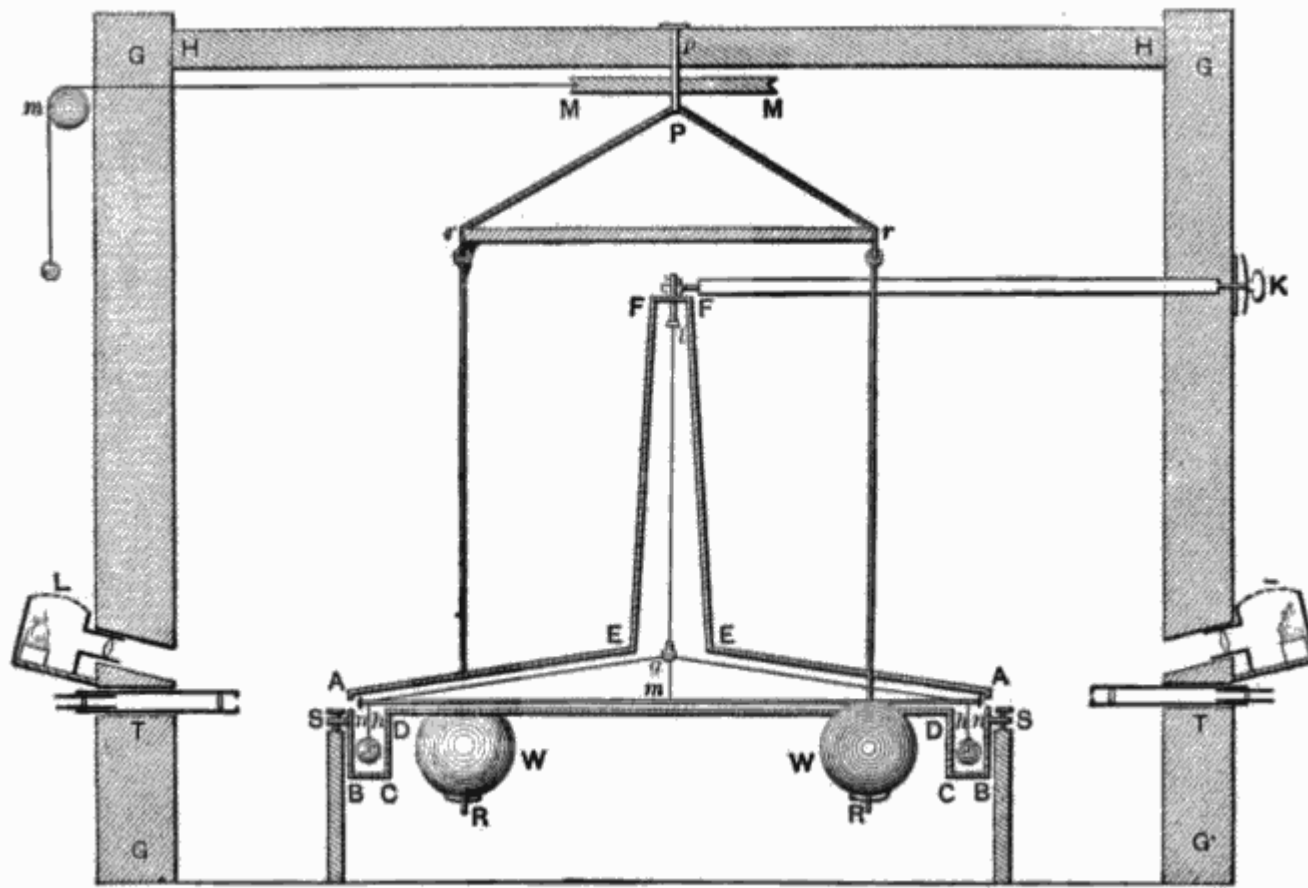
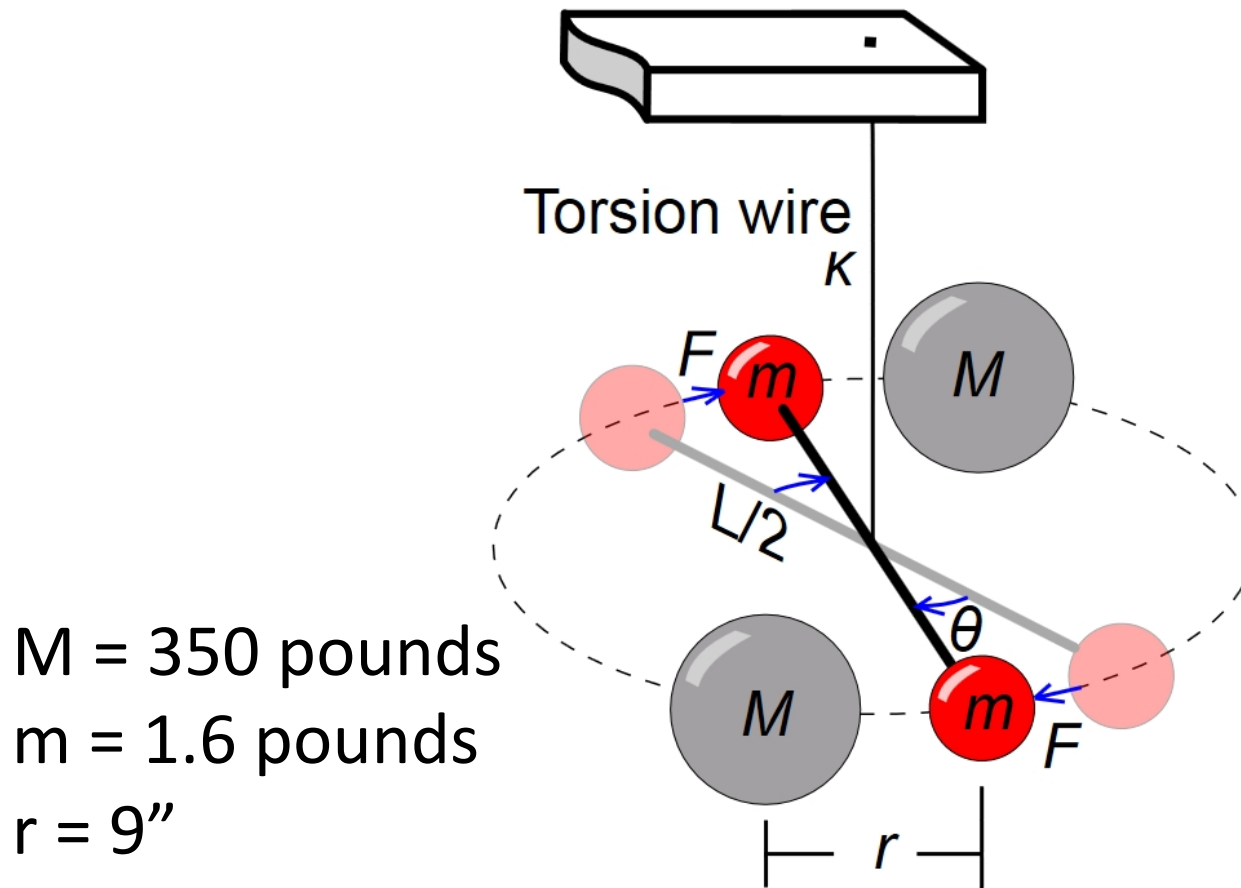


Fig. 1

Cavendish Schematic



$F = 1.7 \times 10^{-7} \text{ N}$ equivalent to 17 micrograms!


$$\begin{aligned} M_E &= gR_E^2/G \\ &= 9.8(6.38 \times 10^6)^2 / 6.67 \times 10^{-11} \text{ (SI units)} \\ &= 6.0 \times 10^{24} \text{ kg} \end{aligned}$$

What are Stars?

Pinprick holes in a colorless sky?

--- *The Moody Blues*

<http://www.wheretowillie.com>



What are they...

where are they...

how far away?

Parallax

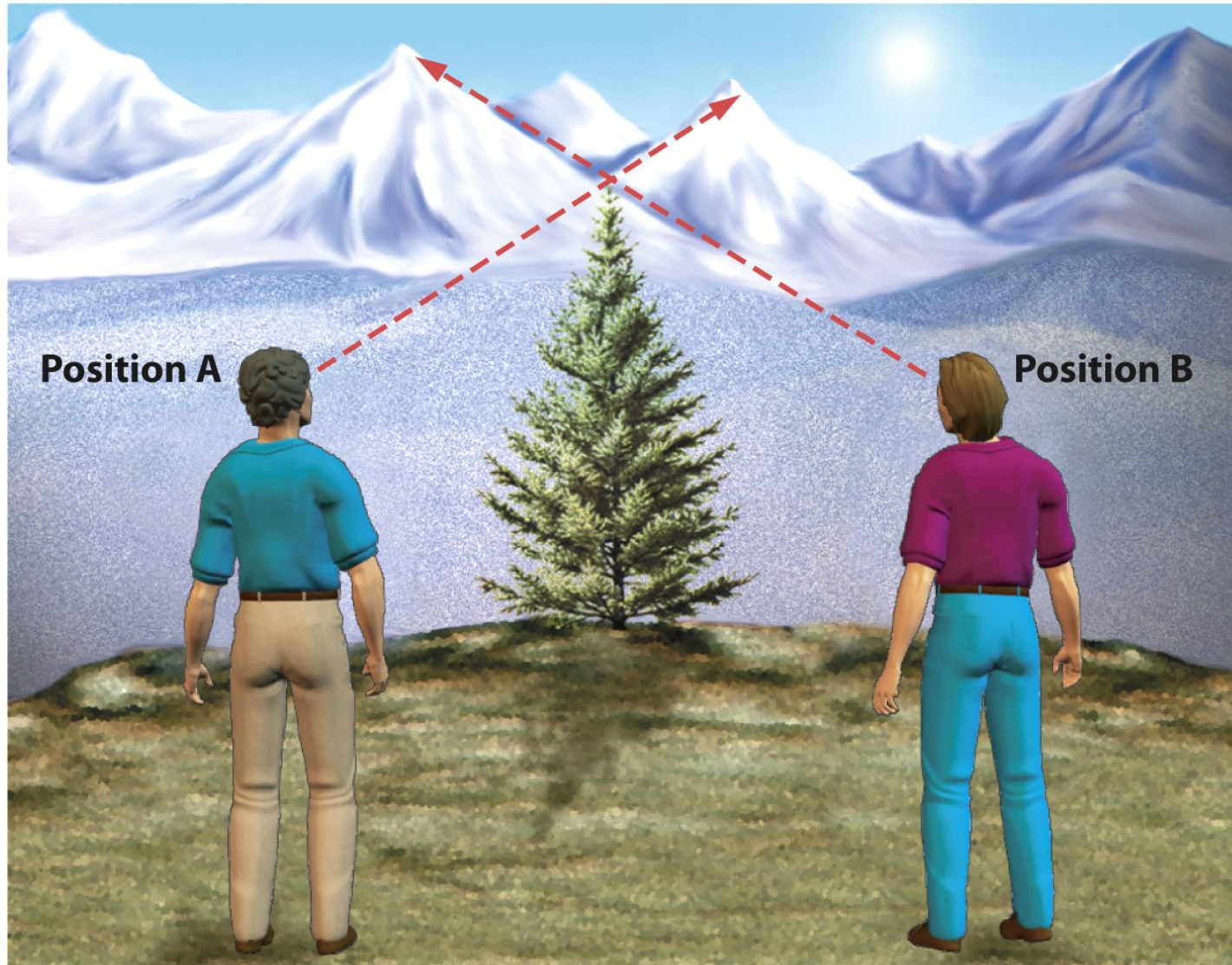
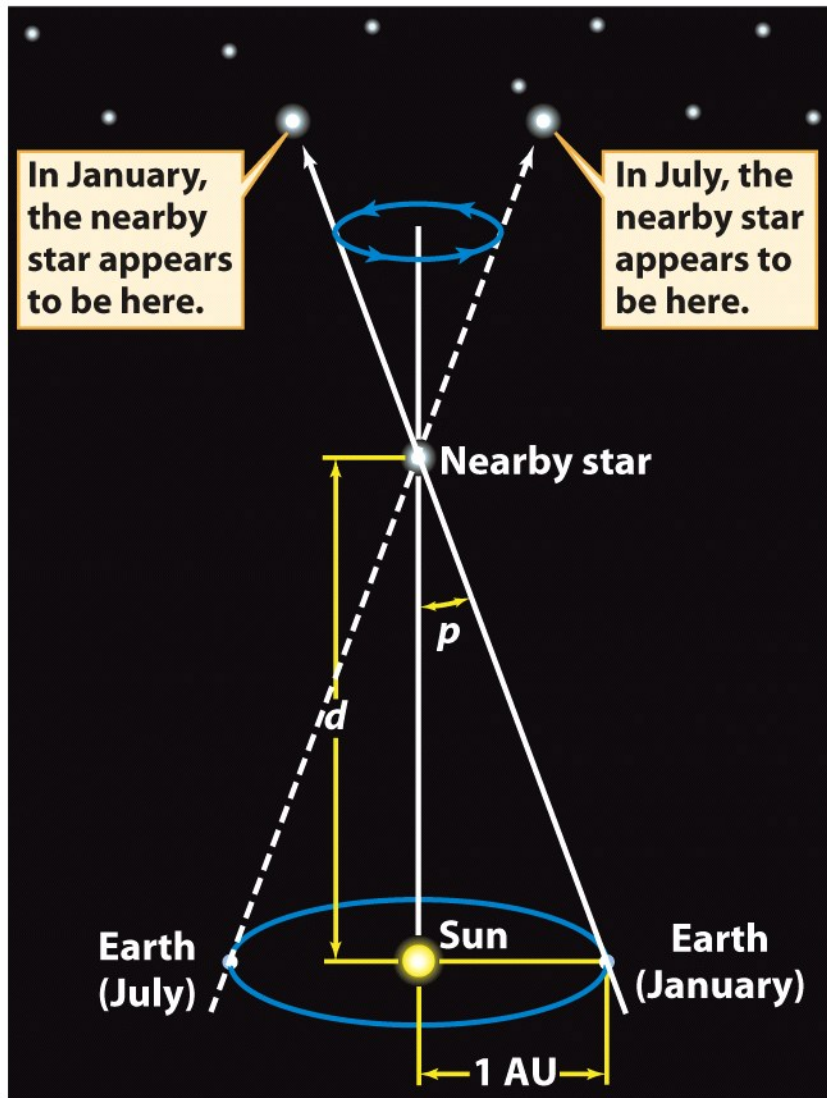
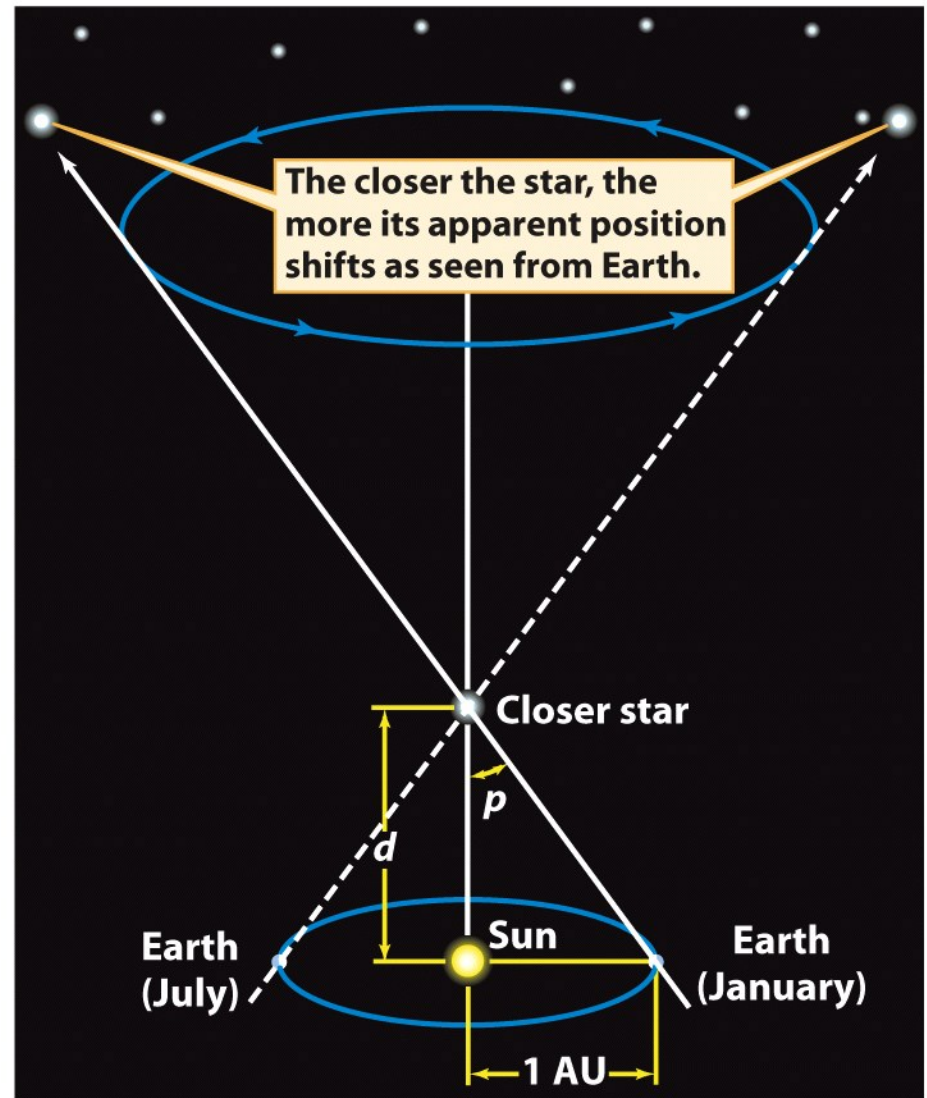


Figure 10-1
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Parallax



(a) Parallax of a nearby star

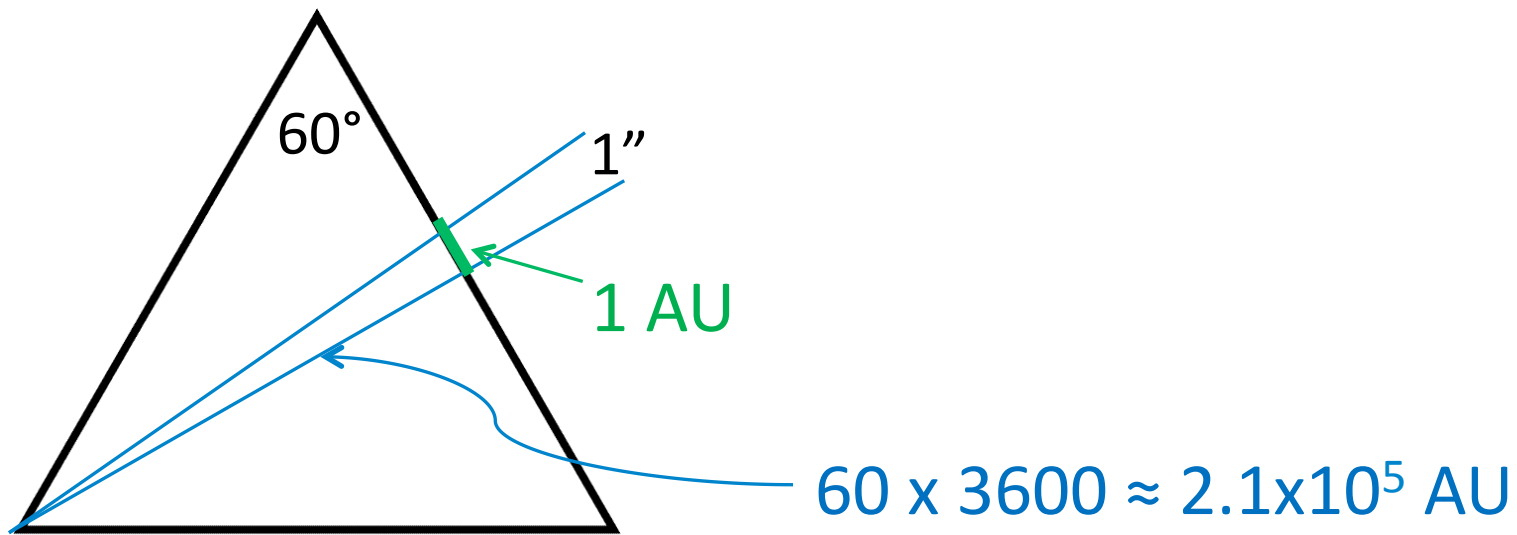


(b) Parallax of an even closer star

All stellar parallax angles are less than one second of arc!

There are 60 sec in a minute and 60 min in a degree

$$1'' = 1/3600 \text{ deg}$$



$$2.1 \times 10^5 \times 93,000,000 \text{ miles} = 2 \times 10^{13} \text{ miles!}$$

$$2 \times 10^{13} / (1.86 \times 10^5 \times 3600 \times 24 \times 365) = 3.3 \text{ years!!}$$

All stars are farther than 3.3 light years away!

The Nearest Stars

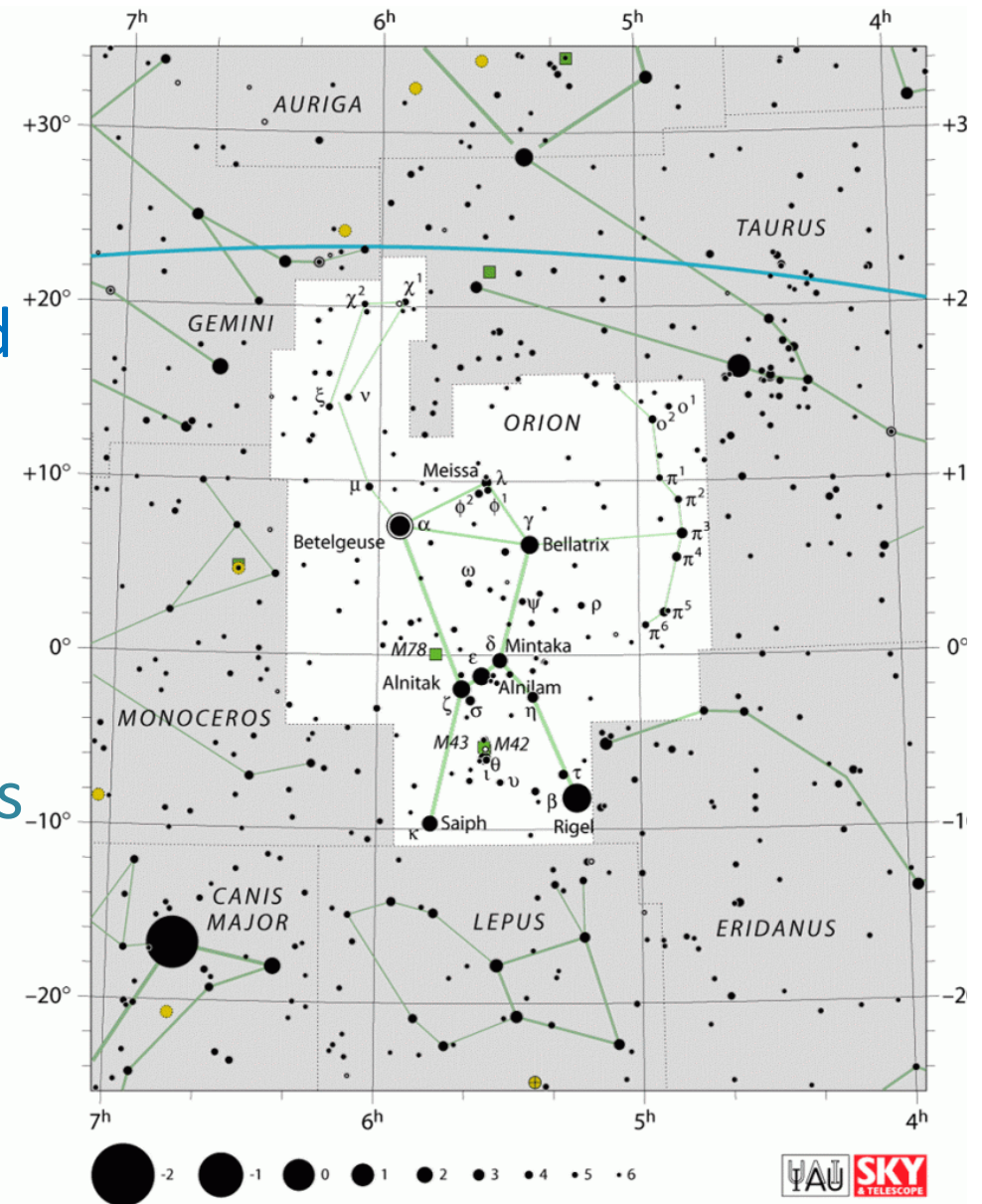
<u>Star</u>	<u>Distance (light years)</u>
Alpha Centauri C (“Proxima”)	4.2
Alpha Centauri A and B	4.3
Barnard’s Star	6.0
Wolf 359	7.7
BD +36 degrees 2147	8.2
Luyten 726-8 A and B	8.4
Sirius A and B	8.6
Ross 154	9.4
Ross 248	10.4
Epsilon Eradinis	10.8
Ross 128	10.9
61 Cygni A and B	11.1
Procyon A and B	11.4

Stellar Brightness

Stellar brightness is measured with apparent magnitude.

The smaller the magnitude, the brighter the star.

Apparent magnitude depends on intrinsic brightness and distance.



Absolute Magnitude (Intrinsic Brightness)

Given

- The apparent magnitude
- The distance
- The inverse square law: $\text{Intensity} \sim 1/(\text{distance})^2$

One can calculate the absolute magnitude
which is the magnitude a star would have if it
was ca. 30 light years (10 parsecs = 32.6 ly) away.

The Brightest Stars

Names		Dist(ly)	App Mag	Abs Mag
<u>Sirius</u>	Alpha <u>C</u> Ma	8.6	-1.46	1.4
<u>Canopus</u>	Alpha <u>C</u> ar	74	-0.72	-2.5
<u>Rigil Kentaurus</u>	Alpha <u>C</u> en	4.3	-0.27	4.4
<u>Arcturus</u>	Alpha <u>B</u> oo	34	-0.04	0.2
<u>Vega</u>	Alpha <u>L</u> yr	25	0.03	0.6
<u>Capella</u>	Alpha <u>A</u> ur	41	0.08	0.4
<u>Rigel</u>	Beta <u>O</u> ri	~1400	0.12	-8.1
<u>Procyon</u>	Alpha <u>C</u> Mi	11.4	0.38	2.6
<u>Achernar</u>	Alpha <u>E</u> ri	69	0.46	-1.3
<u>Betelgeuse</u>	Alpha <u>O</u> ri	~1400	0.50 (var.)	-7.2
<u>Hadar</u>	Beta <u>C</u> en	320	0.61 (var.)	-4.4
<u>Acrux</u>	Alpha <u>C</u> ru	510	0.76	-4.6
<u>Altair</u>	Alpha <u>A</u> ql	16	0.77	2.3
<u>Aldebaran</u>	Alpha <u>T</u> au	60	0.85 (var.)	-0.3
<u>Antares</u>	Alpha <u>S</u> co	~520	0.96 (var.)	-5.2
<u>Spica</u>	Alpha <u>V</u> ir	220	0.98 (var.)	-3.2
<u>Pollux</u>	Beta <u>G</u> em	40	1.14	0.7
<u>Fomalhaut</u>	Alpha <u>P</u> sA	22	1.16	2.0
<u>Becrux</u>	Beta <u>C</u> ru	460	1.25 (var.)	-4.7
<u>Deneb</u>	Alpha <u>C</u> yg	1500	1.25	-7.2
<u>Regulus</u>	Alpha <u>L</u> eo	69	1.35	-0.3
<u>Adhara</u>	Epsilon <u>C</u> Ma	570	1.50	-4.8
<u>Castor</u>	Alpha <u>G</u> em	49	1.57	0.5
<u>Gacrux</u>	Gamma <u>C</u> ru	120	1.63 (var.)	-1.2
<u>Shaula</u>	Lambda <u>S</u> co	330	1.63 (var.)	-3.5

What does brightness depend on?

Size and Temperature

Blackbody Radiation

All dense objects emit electromagnetic radiation at any finite temperature.

The higher the temperature of a blackbody, the shorter the wavelength of maximum emission (the wavelength at which the curve peaks).

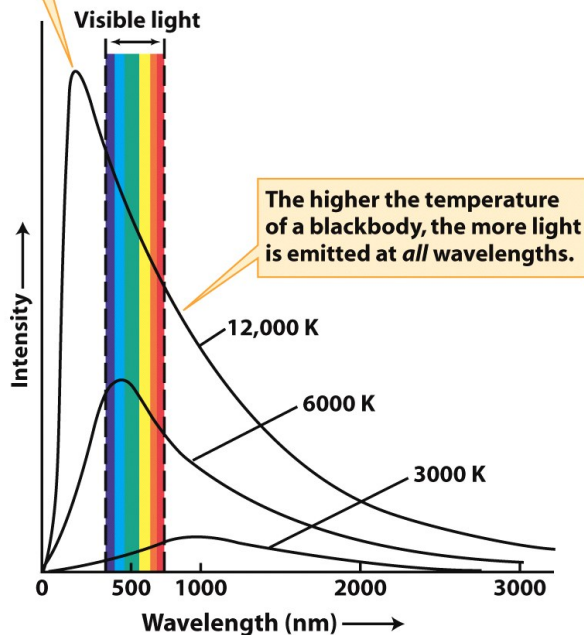
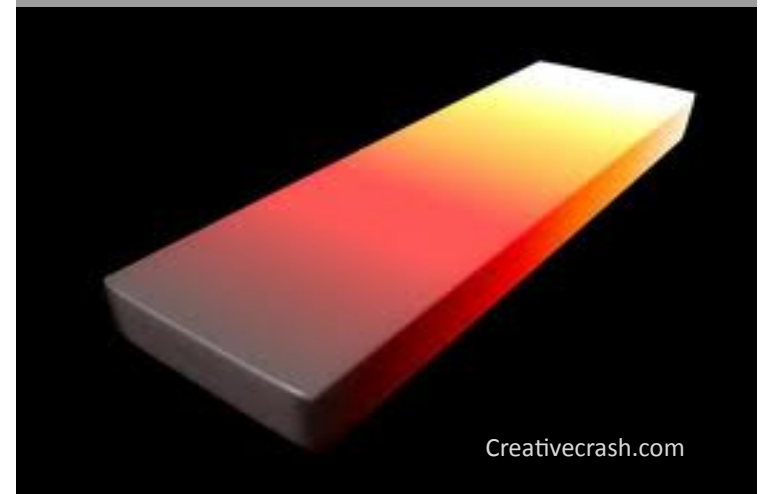
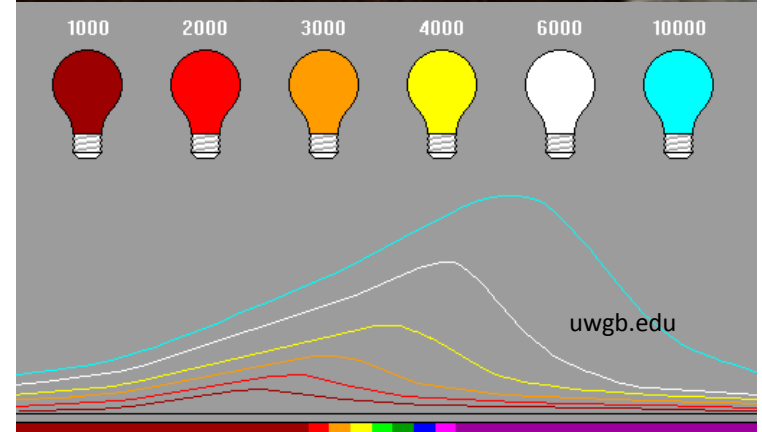


Figure 2-11
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“Bluer” is hotter
“Bluer” is brighter



miraimages.photoshelter.com



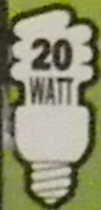
Creativecrash.com



**energy
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a smart way to save energy!®

\$44
IN ENERGY
SAVINGS
PER BULB**



Soft White 2700K

light output:
1200 lumens

energy used:
20 watts

life:
8000 hours

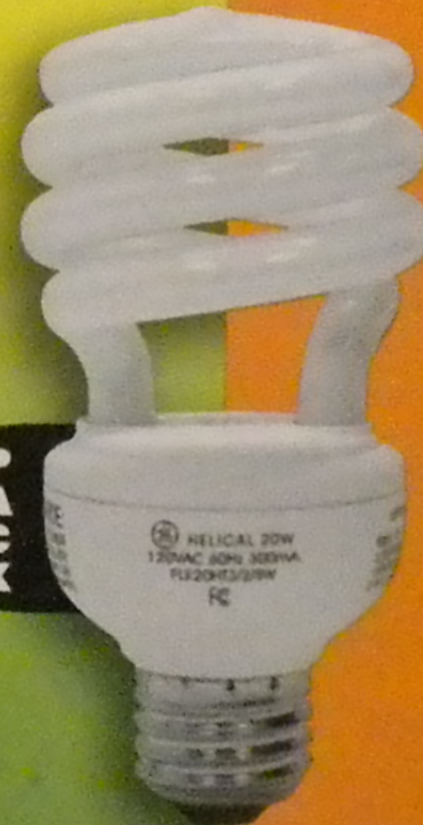
contains:
2 bulbs (Spiral®)

To save energy costs, find the bulbs with the light output you need, then choose the one with the lowest watts.

75

REPLACEMENT
LASTS 5
YEARS*

**2
PACK**

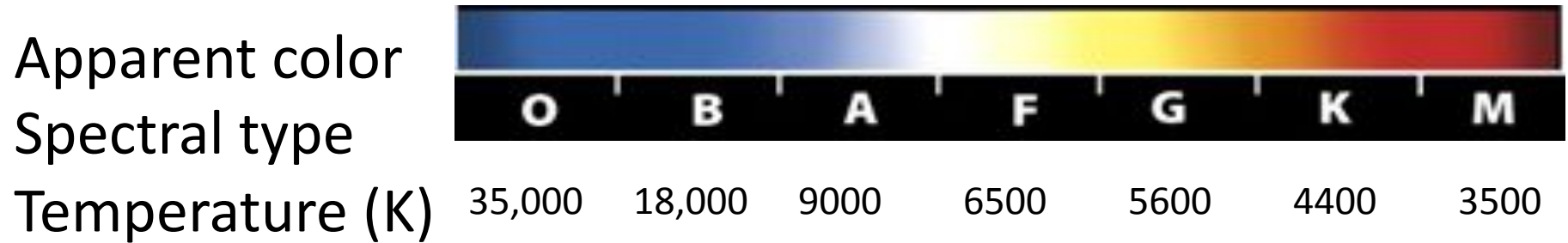


20 WATT



Stars have color,
hence we can measure their temperatures!

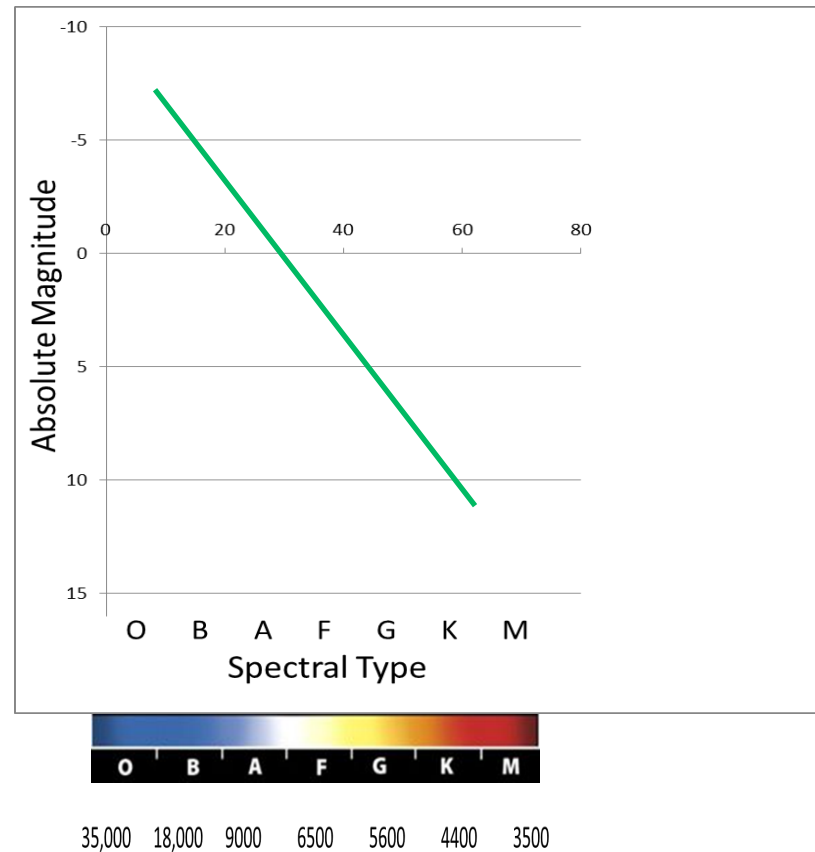
Stellar Temperatures and Spectral Types



Are bluer stars brighter, are redder stars dimmer?

Probably yes.

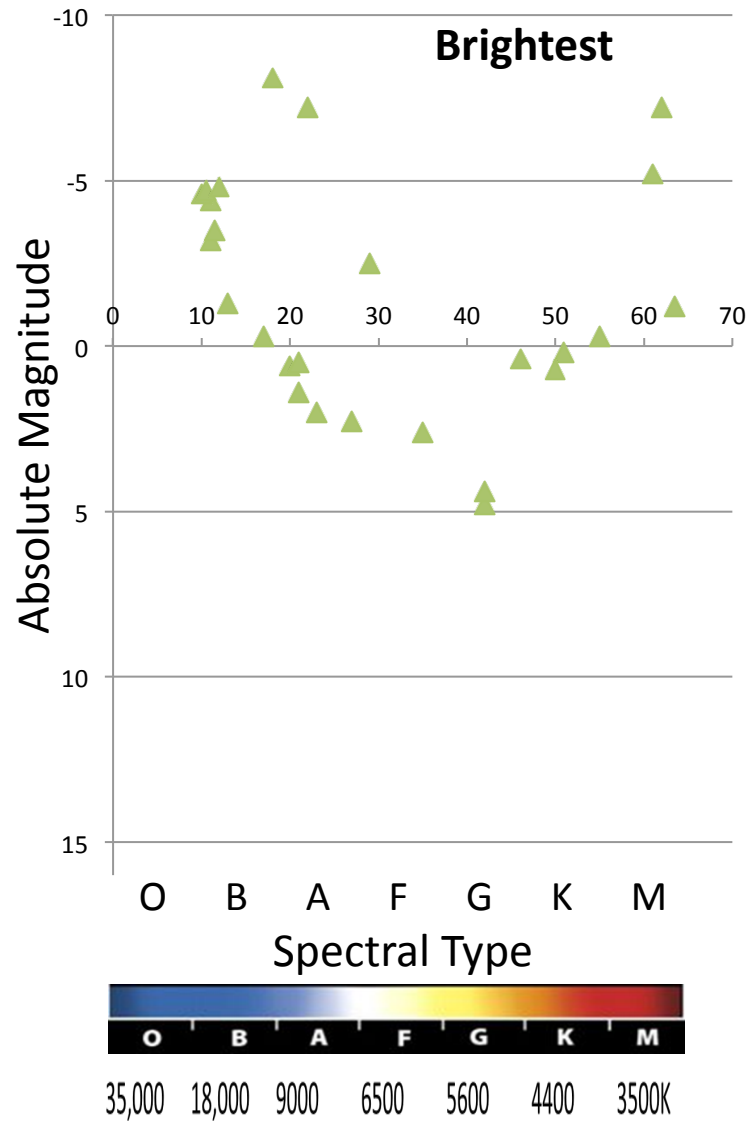
We expect



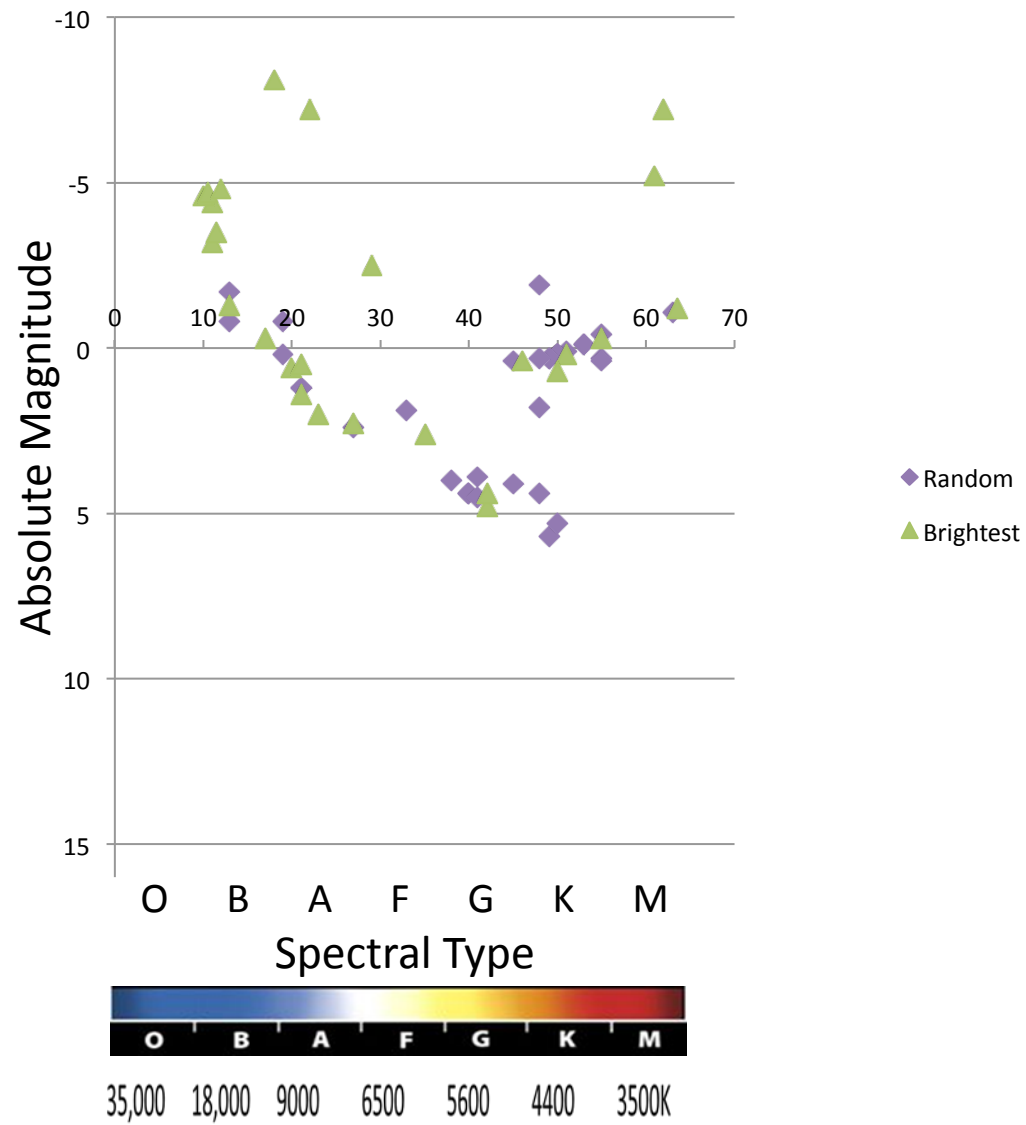
Is this in fact true?

We must test our hypothesis.

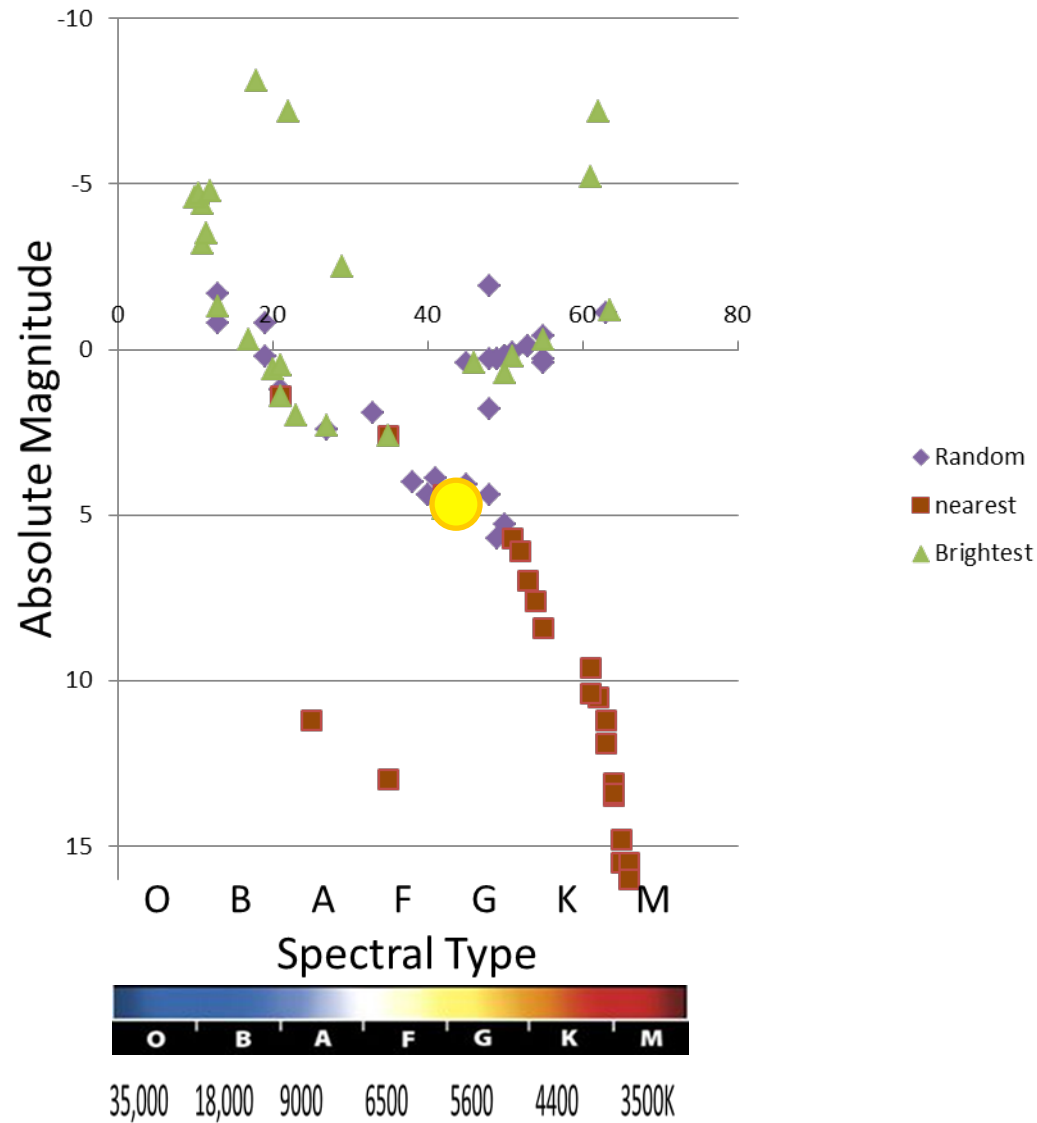
The Brightest Stars



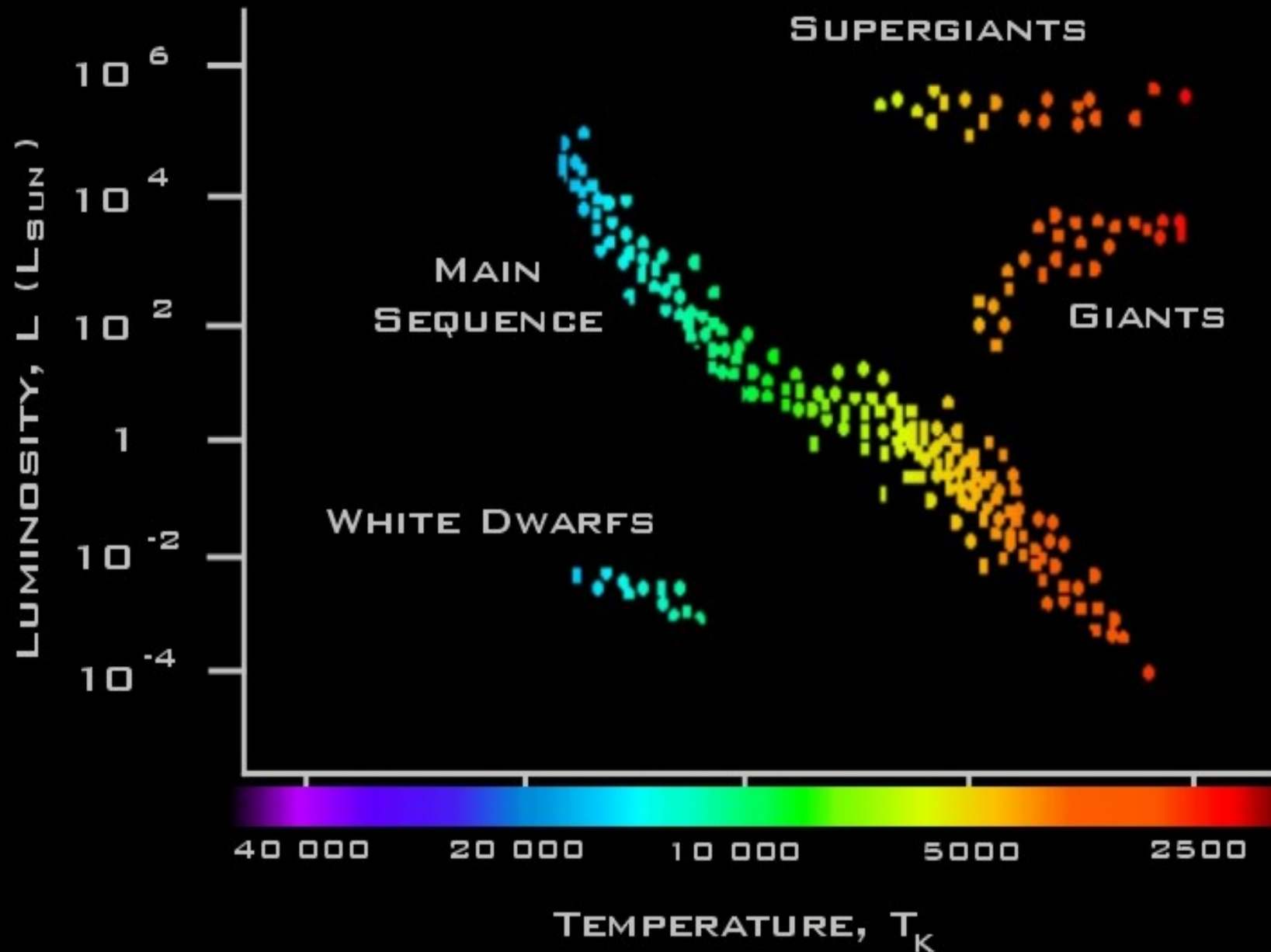
The Brightest and Randomly Picked Stars



The Brightest, Randomly Picked and Nearest Stars



The Hertzsprung-Russell Diagram



And now we find that we have, as Galileo advised, read “Nature like an open book”.

Stars are distant suns, and our Sun is one of many stars, and the possible stars are manifold to include many like our Sun but with widely ranging luminosities, and others that are giants of unimaginable proportions or dwarfs of enormous densities!

Yet, our quest continues (does it ever end?)!

We ask how do they shine? How were they formed?

Do their fires ever extinguish, and if so, how do they die?

These questions and others are accessible
via the method of science

and that's how we know what we know!

The Kinetic Theory of Heat

Boltzmann, ca. 1900

An atom of mass m
has a velocity v given by

$$v^2 = 3kT/m \quad (1)$$

k is Boltzmann's constant

T is the temperature (absolute).

Force due to one atom bounce

$$F = ma = m\Delta v/\Delta t = \Delta p/\Delta t$$

$$F = 2mv/(2L/v) = mv^2/L$$

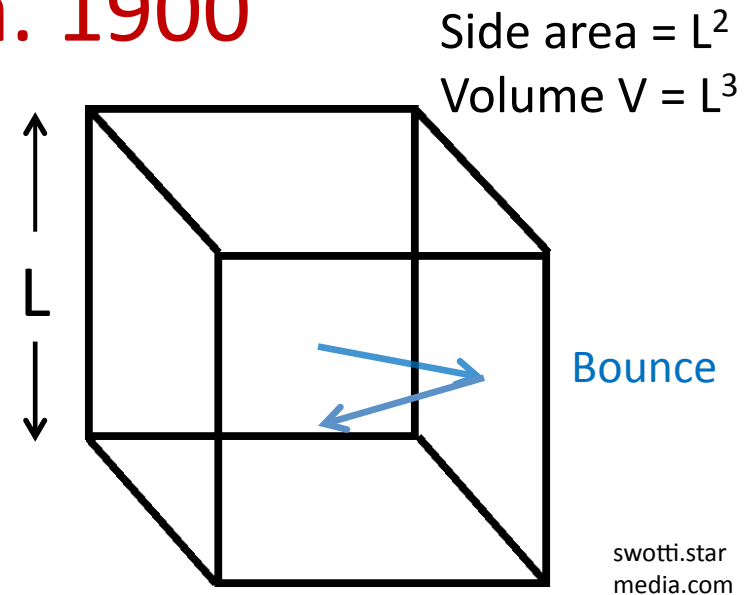
$$\text{Pressure } P = F/L^2 = mv^2/L^3$$

$$P = mv^2/V = 3kT/V$$

$$\text{Total pressure } P = (N/3)3kT/V \implies PV = NkT$$

The Ideal

Gas Law



$$\Delta p = 2p = 2mv$$

Round trip time

$$\Delta t = 2L/v$$

N atoms, $N/3$ moving
along x-direction.